

# Package: smacofx (via r-universe)

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**Title** Flexible Multidimensional Scaling and 'smacof' Extensions

**Version** 1.5-3

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**Description** Flexible multidimensional scaling (MDS) methods and extensions to the package 'smacof'. This package contains various functions, wrappers, methods and classes for fitting, plotting and displaying a large number of different flexible MDS models (some as of yet unpublished). These are: Torgerson scaling (Torgerson, 1958, ISBN:978-0471879459) with powers, Sammon mapping (Sammon, 1969, <[doi:10.1109/T-C.1969.222678](https://doi.org/10.1109/T-C.1969.222678)>) with ratio and interval optimal scaling, Multiscale MDS (Ramsay, 1977, <[doi:10.1007/BF02294052](https://doi.org/10.1007/BF02294052)>) with ratio and interval optimal scaling, S-stress MDS (ALSCAL; Takane, Young & De Leeuw, 1977, <[doi:10.1007/BF02293745](https://doi.org/10.1007/BF02293745)>) with ratio and interval optimal scaling, elastic scaling (McGee, 1966, <[doi:10.1111/j.2044-8317.1966.tb00367.x](https://doi.org/10.1111/j.2044-8317.1966.tb00367.x)>) with ratio and interval optimal scaling, r-stress MDS (De Leeuw, Groenen & Mair, 2016, <<https://rpubs.com/deleeuw/142619>>) with ratio, interval and non-metric optimal scaling, power-stress MDS (POST-MDS; Buja & Swayne, 2002 <[doi:10.1007/s00357-001-0031-0](https://doi.org/10.1007/s00357-001-0031-0)>) with ratio and interval optimal scaling, restricted power-stress (Rusch, Mair & Hornik, 2021, <[doi:10.1080/10618600.2020.1869027](https://doi.org/10.1080/10618600.2020.1869027)>) with ratio and interval optimal scaling, approximate power-stress with ratio optimal scaling (Rusch, Mair & Hornik, 2021, <[doi:10.1080/10618600.2020.1869027](https://doi.org/10.1080/10618600.2020.1869027)>), Box-Cox MDS (Chen & Buja, 2013, <<https://jmlr.org/papers/v14/chen13a.html>>), local MDS (Chen & Buja, 2009, <[doi:10.1198/jasa.2009.0111](https://doi.org/10.1198/jasa.2009.0111)>), curvilinear component analysis (Demartines & Herault, 1997, <[doi:10.1109/72.554199](https://doi.org/10.1109/72.554199)>) and curvilinear distance analysis (Lee, Lendasse & Verleysen, 2004, <[doi:10.1016/j.neucom.2004.01.007](https://doi.org/10.1016/j.neucom.2004.01.007)>). There also are experimental models (e.g., sparsified MDS and sparsified POST-MDS). Some functions are suitably flexible to allow any other sensible combination of explicit power transformations

for weights, distances and input proximities with implicit ratio, interval or non-metric optimal scaling of the input proximities. Most functions use a Majorization-Minimization algorithm. Currently the methods are only available for one-mode data (symmetric dissimilarity matrices).

**Depends** R (>= 3.5.0), smacof (>= 1.10-4)

**Imports** MASS, minqa, plotrix, ProjectionBasedClustering, weights, vegan

**License** GPL-2 | GPL-3

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**URL** <https://r-forge.r-project.org/projects/stops/>

**BugReports**

[https://r-forge.r-project.org/tracker/?atid=5375&group\\_id=2037&func=browse](https://r-forge.r-project.org/tracker/?atid=5375&group_id=2037&func=browse)

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<b>alscal</b>	<i>ALSCAL - MDS via S-Stress Minimization</i>
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---

## Description

An implementation to minimize s-stress by majorization with ratio and interval optimal scaling.

## Usage

```
alscal(
  delta,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)
```

## Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances
type	what type of MDS to fit. Currently one of "ratio" or "interval". Default is "ratio".
weightmat	a matrix of finite weights
init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.

<code>itmax</code>	maximum number of iterations. Default is 10000.
<code>verbose</code>	should iteration output be printed; if > 1 then yes
<code>principal</code>	If ‘TRUE’, principal axis transformation is applied to the final configuration

**Value**

a ‘smacofP’ object (inheriting from ‘smacofB’, see [smacofSym](#)). It is a list with the components

- `delta`: Observed untransformed dissimilarities
- `tdelta`: Observed explicitly transformed (squared) dissimilarities, normalized
- `dhat`: Explicitly transformed dissimilarities (`dhats`), optimally scaled and normalized
- `confdist`: Configuration dissimilarities
- `conf`: Matrix of fitted configuration
- `stress`: Default stress (stress 1; sqrt of explicitly normalized stress)
- `spp`: Stress per point
- `ndim`: Number of dimensions
- `model`: Name of smacof model
- `niter`: Number of iterations
- `nobj`: Number of objects
- `type`: Type of MDS model
- `weightmat`: weighting matrix as supplied
- `stress.m`: Default stress (stress-1^2)
- `tweightmat`: transformed weighting matrix (here NULL)

**See Also**

[rStressMin](#)

**Examples**

```
dis<-smacof::kinshipdelta
res<-alscal(as.matrix(dis),type="interval",itmax=1000)
res
summary(res)
plot(res)
```

---

apStressMin	<i>Approximate Power Stress MDS</i>
-------------	-------------------------------------

---

## Description

An implementation to minimize approximate power stress by majorization with ratio or interval optimal scaling. This approximates the power stress objective in such a way that it can be fitted with SMACOF without distance transformations. See Rusch et al. (2021) for details.

## Usage

```
apStressMin(  
  delta,  
  kappa = 1,  
  lambda = 1,  
  nu = 1,  
  type = "ratio",  
  weightmat = 1 - diag(nrow(delta)),  
  init = NULL,  
  ndim = 2,  
  acc = 1e-06,  
  itmax = 10000,  
  verbose = FALSE,  
  principal = FALSE  
)  
  
apowerstressMin(  
  delta,  
  kappa = 1,  
  lambda = 1,  
  nu = 1,  
  type = "ratio",  
  weightmat = 1 - diag(nrow(delta)),  
  init = NULL,  
  ndim = 2,  
  acc = 1e-06,  
  itmax = 10000,  
  verbose = FALSE,  
  principal = FALSE  
)  
  
apostmds(  
  delta,  
  kappa = 1,  
  lambda = 1,  
  nu = 1,  
  type = "ratio",
```

```

weightmat = 1 - diag(nrow(delta)),
init = NULL,
ndim = 2,
acc = 1e-06,
itmax = 10000,
verbose = FALSE,
principal = FALSE
)

apstressMin(
  delta,
  kappa = 1,
  lambda = 1,
  nu = 1,
  type = "ratio",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

apstressmds(
  delta,
  kappa = 1,
  lambda = 1,
  nu = 1,
  type = "ratio",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

```

## Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances
kappa	power of the transformation of the fitted distances; defaults to 1
lambda	the power of the transformation of the proximities; defaults to 1
nu	the power of the transformation for weightmat; defaults to 1
type	what type of MDS to fit. Only "ratio" currently.
weightmat	a binary matrix of finite nonnegative weights.

init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.
itmax	maximum number of iterations. Default is 10000.
verbose	should iteration output be printed; if > 1 then yes
principal	If 'TRUE', principal axis transformation is applied to the final configuration

### Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- delta: Observed, untransformed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized
- dhat: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- stress.m: Default stress (stress-1^2)
- tweightmat: transformed weighting matrix (here weightmat^nu)

### Note

Internally we calculate the approximation parameters  $\text{upsilon}=\text{nu}+2*\lambda*(1-(1/\kappa))$  and  $\tau=\lambda/\kappa$ . They are not output.

### References

Rusch, Mair, Hornik (2021). Cluster Optimized Proximity Scaling. JCGS <[doi:10.1080/10618600.2020.1869027](https://doi.org/10.1080/10618600.2020.1869027)>

### Examples

```
dis<-smacof::kinshipdelta
res<-apStressMin(as.matrix(dis),kappa=2,lambda=1.5,itmax=1000)
res
summary(res)
plot(res)
plot(res,"Shepard")
plot(res,"transplot")
```

---

**BankingCrisesDistances***Banking Crises Distances*

---

**Description**

Matrix of Jaccard distances between 70 countries (Hungary and Greece were combined to be the same observation) based on their binary time series of having had a banking crises in a year from 1800 to 2010 or not. See `data(bankingCrises)` in package `Ecdat` for more info. The last column is Reinhart & Rogoffs classification as a low (3), middle- (2) or high-income country (1).

**Format**

A 69 x 70 matrix.

**Source**

`data(bankingCrises)` in library(`Ecdat`)

---

**bcmds***Box-Cox MDS*

---

**Description**

This function minimizes the Box-Cox Stress of Chen & Buja (2013) via gradient descent. This is a ratio metric scaling method. The transformations are not straightforward to interpret but mu is associated with fitted distances in the configuration and lambda with the dissimilarities. Concretely for fitted distances (attraction part) it is  $BC_{mu+lambda}(d(X))$  and for the repulsion part it is  $delta^lambda BC_{mu}(d(X))$  with BC being the one-parameter Box-Cox transformation.

**Usage**

```
bcmds(
  delta,
  mu = 1,
  lambda = 1,
  rho = 0,
  type = "ratio",
  ndim = 2,
  weightmat = 1 - diag(nrow(delta)),
  itmax = 2000,
  init = NULL,
  verbose = 0,
  addD0 = 1e-04,
  principal = FALSE,
```

```
    normconf = FALSE
)

bcStressMin(
  delta,
  mu = 1,
  lambda = 1,
  rho = 0,
  type = "ratio",
  ndim = 2,
  weightmat = 1 - diag(nrow(delta)),
  itmax = 2000,
  init = NULL,
  verbose = 0,
  addD0 = 1e-04,
  principal = FALSE,
  normconf = FALSE
)

bcstressMin(
  delta,
  mu = 1,
  lambda = 1,
  rho = 0,
  type = "ratio",
  ndim = 2,
  weightmat = 1 - diag(nrow(delta)),
  itmax = 2000,
  init = NULL,
  verbose = 0,
  addD0 = 1e-04,
  principal = FALSE,
  normconf = FALSE
)

boxcoxmds(
  delta,
  mu = 1,
  lambda = 1,
  rho = 0,
  type = "ratio",
  ndim = 2,
  weightmat = 1 - diag(nrow(delta)),
  itmax = 2000,
  init = NULL,
  verbose = 0,
  addD0 = 1e-04,
  principal = FALSE,
```

```
normconf = FALSE
)
```

## Arguments

<code>delta</code>	dissimilarity or distance matrix, dissimilarity or distance data frame or 'dist' object
<code>mu</code>	mu parameter. Should be 0 or larger for everything working ok. If mu<0 it works but I find the MDS model is strange and normalized stress tends towards 0 regardless of fit. Use normalized stress at your own risk in that case.
<code>lambda</code>	lambda parameter. Must be larger than 0.
<code>rho</code>	the rho parameter, power for the weights (called nu in the original article).
<code>type</code>	what type of MDS to fit. Only "ratio" currently.
<code>ndim</code>	the dimension of the configuration
<code>weightmat</code>	a matrix of finite weights. Not implemented.
<code>itmax</code>	number of optimizing iterations, defaults to 2000.
<code>init</code>	initial configuration. If NULL a classical scaling solution is used.
<code>verbose</code>	prints progress if > 3.
<code>addD0</code>	a small number that's added for D(X)=0 for numerical evaluation of worst fit (numerical reasons, see details). If addD0=0 the normalized stress for mu!=0 and mu+lambda!=0 is correct, but will give useless normalized stress for mu=0 or mu+lambda!=0.
<code>principal</code>	If 'TRUE', principal axis transformation is applied to the final configuration
<code>normconf</code>	normalize the configuration to sum(delta^2)=1 (as in the power stresses). Default is FALSE. Note that then the distances in confdist do not match manually calculated ones.

## Details

For numerical reasons with certain parameter combinations, the normalized stress uses a configuration as worst result where every d(X) is 0+addD0. The same number is not added to the delta so there is a small inaccuracy of the normalized stress (but negligible if min(delta)>>addD0). Also, for mu<0 or mu+lambda<0 the normalization cannot generally be trusted (in the worst case of D(X)=0 one would have an 0^(-a)).

## Value

an object of class 'bcmds' (also inherits from 'smacofP'). It is a list with the components

- `delta`: Observed, untransformed dissimilarities
- `tdelta`: Observed explicitly transformed dissimilarities, normalized
- `dhat`: Explicitly transformed dissimilarities (dhats)
- `confdist`: Configuration dissimilarities
- `conf`: Matrix of fitted configuration

- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- ndim: Number of dimensions
- model: Name of MDS model
- type: Must be "ratio" here.
- niter: Number of iterations
- nobj: Number of objects
- pars: hyperparameter vector theta
- weightmat: 1-diagonal matrix. For compatibility with smacofP classes.
- parameters, pars, theta: The parameters supplied
- call the call

and some additional components

- stress.m: default stress is the explicitly normalized stress on the normalized, transformed dissimilarities
- mu: mu parameter (for attraction)
- lambda: lambda parameter (for repulsion)
- rho: rho parameter (for weights)

### Author(s)

Lisha Chen & Thomas Rusch

### Examples

```
dis<-smacof::kinshipdelta
res<-bcmds(dis,mu=2,lambda=1.5,rho=0)
res
summary(res)
plot(res)
```

bcsdistance

*Calculates the blended Chi-square distance matrix between n vectors*

### Description

The pairwise blended chi-distance of two vectors x and y is  $\sqrt{\text{sum}(((x[i]-y[i])^2)/(2*(ax[i]+by[i])))}$ , with originally a in [0,1] and b=1-a as in Lindsay (1994) (but we allow any non-negative a and b). The function calculates this for all pairs of rows of a matrix or data frame x.

### Usage

```
bcsdistance(x, a = 0.5, b = 1 - a)
```

### Arguments

- x an n times p numeric matrix or data frame. Note that the values of x must be non-negative.
- a first blending weight. Must be non-negative and should be in [0,1] if a blended chi-square distance as in Lindsay (1994) is sought. Defaults to 0.5.
- b second blending weight. Must be non-negative and should be 1-a if a blended chi-square distance as in Lindsay (1994) is sought. Defaults to 1-a.

### Value

a symmetric n times n matrix of pairwise blended chi-square distance (between rows of x) with 0 in the main diagonal. It is an object of class distance and matrix with attributes "method", "type" and "par", the latter returning the a and b values.

### References

Lindsay (1994). Efficiency versus robustness: the case for minimum Hellinger distance and related methods. Annals of Statistics, 22 (2), 1081-1114. <doi:10.1214/aos/1176325512>

**biplotmds.smacofP**      *S3 method for smacofP objects*

### Description

S3 method for smacofP objects

### Usage

```
## S3 method for class 'smacofP'
biplotmds(object, extvar, scale = TRUE)
```

### Arguments

- object An object of class smacofP
- extvar Data frame with external variables.
- scale if 'TRUE' external variables are standardized internally.

### Details

If a model for individual differences is provided, the external variables are regressed on the group stimulus space configurations. For objects returned from 'biplotmds' we use the plot method in **biplotmds**. In the biplot called with plot() only the relative length of the vectors and their direction matters. Using the vecscale argument in plot() the user can control for the relative length of the vectors. If 'vecscale = NULL', the 'vecscale()' function from the 'candisc' package is used which tries to automatically calculate the scale factor so that the vectors approximately fill the same space as the configuration. In this method vecscale should usually be smaller than the one used in smacof by a factor of 0.1.

## Value

Returns an object belonging to classes 'mlm' and 'mdsbi'. See 'lm' for details. R2vec: Vector containing the R2 values. See also [biplotmds](#) for the plot method.

## Examples

```
## see smacof::biplotmds for more
res <- powerStressMin(morse,kappa=0.5,lambda=2)
fitbi <- biplotmds(res, morsescales[,2:3])
plot(fitbi, main = "MDS Biplot", vecscale = 0.03)
```

bootmds.smacofP

*MDS Bootstrap for smacofP objects*

## Description

Performs a bootstrap on an MDS solution. It works for derived dissimilarities only, i.e. generated by the call `dist(data)`. The original data matrix needs to be provided, as well as the type of dissimilarity measure used to compute the input dissimilarities.

## Usage

```
## S3 method for class 'smacofP'
bootmds(
  object,
  data,
  method.dat = "pearson",
  nrep = 100,
  alpha = 0.05,
  verbose = FALSE,
  ...
)
```

## Arguments

<code>object</code>	Object of class <code>smacofP</code> if used as method or another object inheriting from <code>smacofB</code> (needs to be called directly as <code>bootmds.smacofP</code> then).
<code>data</code>	Initial data (before dissimilarity computation).
<code>method.dat</code>	Dissimilarity computation used as MDS input. This must be one of "pearson", "spearmann", "kendall", "euclidean", "maximum", "manhattan", "canberra", "binary".
<code>nrep</code>	Number of bootstrap replications.
<code>alpha</code>	Alpha level for confidence ellipsoids.
<code>verbose</code>	If 'TRUE', bootstrap index is printed out.
<code>...</code>	Additional arguments needed for dissimilarity computation as specified in <a href="#">sim2diss</a> .

## Details

In order to examine the stability solution of an MDS, a bootstrap on the raw data can be performed. This results in confidence ellipses in the configuration plot. The ellipses are returned as list which allows users to produce (and further customize) the plot by hand. See [bootmds](#) for more.

## Value

An object of class 'smacofboot', see [bootmds](#). With values

- cov: Covariances for ellipse computation
- bootconf: Configurations bootstrap samples
- stressvec: Bootstrap stress values
- bootci: Stress bootstrap percentile confidence interval
- spp: Stress per point (based on stress.en)
- stab: Stability coefficient

## Examples

```
##see ?smacof::bootmds for more
data <- na.omit(smacof::PVQ40[,1:5])
diss <- dist(t(data)) ## Euclidean distances
fit <- rStressMin(diss,r=0.5,itmax=1000) ## 2D ratio MDS
set.seed(123)
resboot <- bootmds(fit, data, method.dat = "euclidean", nrep = 10) #run for more nrep
resboot
plot(resboot) #see ?smacof::bootmds for more on the plot method
```

## Description

Classical Scaling

## Usage

`cmds(Do)`

## Arguments

Do	dissimilarity matrix
----	----------------------

---

**cmdscale***Wrapper to cmdscale for S3 class*

---

## Description

Wrapper to cmdscale for S3 class

## Usage

```
cmdscale(d, k = 2, eig = FALSE, ...)
```

## Arguments

- |     |  |
|-----|--|
| d   | a distance structure such as that returned by 'dist' or a full symmetric matrix containing the dissimilarities |
| k   | the maximum dimension of the space which the data are to be represented in                                     |
| eig | indicates whether eigenvalues should be returned. Defaults to TRUE.  |
| ... | additional parameters passed to cmdscale. See <a href="#">cmdscale</a>   |

## Details

overloads stats::cmdscale turns on the liosting and adds slots and class attributes for which there are methods.

## Value

Object of class 'cmdscalex' and 'cmdscale' extending [cmdscale](#). This wrapper always returns the results of cmdscale as a list, adds column labels to the \$points and adds extra elements (conf=points, delta=d, confdist=dist(conf), dhat=d) and the call to the list, and assigns S3 class 'cmdscalex' and 'cmdscale'.

## Examples

```
dis<-as.matrix(smacof::kinshipdelta)
res<-cmdscale(dis)
```

conf\_adjust

*conf\_adjust: a function to procrustes adjust two matrices***Description**

conf\_adjust: a function to procrustes adjust two matrices

**Usage**

```
conf_adjust(conf1, conf2, verbose = FALSE, eps = 1e-12, itmax = 100)
```

**Arguments**

conf1	reference configuration, a numeric matrix
conf2	another configuration, a numeric matrix
verbose	should adjustment be output; default to FALSE
eps	numerical accuracy
itmax	maximum number of iterations

**Value**

a list with 'ref.conf' being the reference configuration, 'other.conf' the adjusted configuration and 'comparison.conf' the comparison configuration

doubleCenter

*Double centering of a matrix***Description**

Double centering of a matrix

**Usage**

```
doubleCenter(x)
```

**Arguments**

x	numeric matrix
---	----------------

**Value**

the double centered matrix

---

<code>elscal</code>	<i>Elastic Scaling SMACOF</i>
---------------------	-------------------------------

---

### Description

An implementation to minimize elastic scaling stress by majorization with ratio and interval optimal scaling. Uses a repeat loop.

### Usage

```
elscal(
  delta,
  type = c("ratio", "interval"),
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)
```

### Arguments

<code>delta</code>	dist object or a symmetric, numeric data.frame or matrix of distances
<code>type</code>	what type of MDS to fit. Currently one of "ratio" and "interval". Default is "ratio".
<code>weightmat</code>	a matrix of finite weights
<code>init</code>	starting configuration
<code>ndim</code>	dimension of the configuration; defaults to 2
<code>acc</code>	numeric accuracy of the iteration. Default is 1e-6.
<code>itmax</code>	maximum number of iterations. Default is 10000.
<code>verbose</code>	should iteration output be printed; if > 1 then yes
<code>principal</code>	If 'TRUE', principal axis transformation is applied to the final configuration

### Value

a 'smacofP' object (inheriting from smacofB, see [smacofSym](#)). It is a list with the components

- `delta`: Observed untransformed dissimilarities
- `tdelta`: Observed explicitly transformed dissimilarities, normalized
- `dhat`: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- `confdist`: Configuration dissimilarities, NOT normalized
- `conf`: Matrix of fitted configuration, NOT normalized

- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point (based on stress.en)
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- tweightmat: transformed weighting matrix (here weightmat/delta^2)
- stress.m: Default stress (stress-1^2)

### See Also

[rStressMin](#)

### Examples

```
dis<-smacof::kinshipdelta
res<-elscal(as.matrix(dis),itmax=1000)
res
summary(res)
plot(res)
```

*enorm*

*Explicit Normalization Normalizes distances*

### Description

Explicit Normalization Normalizes distances

### Usage

```
enorm(x, w = 1)
```

### Arguments

x	numeric matrix
w	weight

### Value

a constant

---

icExploreGen*Exploring initial configurations in an agnostic way*

---

**Description**

Allows to user to explore the effect of various starting configurations when fitting an MDS model. This is a bit more general than the icExplore function in smacof, as we allow any PS model to be used as the model is either setup by call or by a prefitted object (for the models in cops and stops we do not have a single UI function which necessitates this). Additionally, one can supply their own configurations and not just random ones.

**Usage**

```
icExploreGen(
  object,
  mdscall = NULL,
  conflist,
  nrep = 100,
  ndim,
  returnfit = FALSE,
  min = -5,
  max = 5,
  verbose = FALSE
)
```

**Arguments**

object	A fitted object of class 'smacofP', 'smacofB' or 'smacof'. If supplied this takes precedence over the call argument. If given this is added to the output and may be the optimal one.
mdscall	Alternatively to a fitted object, one can pass a syntactically valid call for any of the MDS functions cops, stops or smacof that find a configuration (not the ones that do parameter selection like pcops or stops). If object and call is given, object takes precedence.
conflist	Optional list of starting configurations.
nrep	If conflist is not supplied, how many random starting configurations should be used.
ndim	Dimensions of target space.
returnfit	Should all fitted MDS be returned. If FALSE (default) none is returned.
min	lower bound for the uniform distribution to sample from
max	upper bound for the uniform distribution to sample from
verbose	If >0 prints the fitting progress.

## Details

If no configuration list is supplied, then nrep configurations are simulated. They are drawn from a ndim-dimensional uniform distribution with minimum min and maximum max. We recommend to use the route via supplying a fitted model as these are typically starting from a Torgerson configuration and are likely quite good.

## Value

an object of class 'icexplore', see **icExplore** for more. There is a plot method in package 'smacof'.

## Examples

```
dis<-kinshipdelta

## Version 1: Using a fitted object (recommended)
res1<-rStressMin(dis,type="ordinal",itmax=100)
resm<-icExploreGen(res1,nrep=5)

## Version 2: Using a call object and supplying conflist
conflist<-list(res1$init,jitter(res1$init,1),jitter(res1$init,1),jitter(res1$init,1))
c1 <- call("smds",delta=dis,tau=0.2,itmax=100)
resm<-icExploreGen(mdscall=c1,conflist=conflist,returnfit=TRUE)

plot(resm)
```

## Description

These functions perform an MDS Jackknife and plot the corresponding solution.

## Usage

```
## S3 method for class 'smacofP'
jackmds(object, eps = 1e-06, itmax = 100, verbose = FALSE)
```

## Arguments

<b>object</b>	Object of class smacofP if used as method or another object inheriting from smacofB (needs to be called directly as jackmds.smacofP then).
<b>eps</b>	Convergence criterion
<b>itmax</b>	Maximum number of iterations
<b>verbose</b>	If 'TRUE', intermediate stress is printed out.

## Details

In order to examine the stability solution of an MDS, a Jackknife on the configurations can be performed (see de Leeuw & Meulman, 1986) and plotted. The plot shows the jackknife configurations which are connected to their centroid. In addition, the original configuration (transformed through Procrustes) is plotted. The Jackknife function itself returns also a stability measure (as ratio of between and total variance), a measure for cross validity, and the dispersion around the original smacof solution.

## Value

An object of class 'smacofJK', see [jackmds](#). With values

- smacof.conf: Original configuration
- jackknife.confboot: An array of n-1 configuration matrices for each Jackknife MDS solution
- comparison.conf: Centroid Jackknife configurations (comparison matrix)
- cross: Cross validity
- stab: Stability coefficient
- disp: Dispersion
- loss: Value of the loss function (just used internally)
- ndim: Number of dimensions
- call: Model call
- niter: Number of iterations
- nobj: Number of objects

## Examples

```
dat <- na.omit(smacof::PVQ40[,1:5])
diss <- dist(t(dat))    ## Euclidean distances
fit <- rStressMin(diss,type="ordinal",r=0.4,itmax=1000) ## 2D ordinal MDS

res.jk <- jackmds(fit)
plot(res.jk, col.p = "black", col.l = "gray")
plot(res.jk, hclpar = list(c = 80, l = 40))
plot(res.jk, hclpar = list(c = 80, l = 40), plot.lines = FALSE)
```

## Description

This function minimizes the Local MDS Stress of Chen & Buja (2006) via gradient descent. This is a ratio metric scaling method.

## Usage

```
lmds(
  delta,
  k = 2,
  tau = 1,
  type = "ratio",
  ndim = 2,
  weightmat = 1 - diag(nrow(delta)),
  itmax = 5000,
  init = NULL,
  verbose = 0,
  principal = FALSE,
  normconf = FALSE
)
```

## Arguments

delta	dissimilarity or distance matrix, dissimilarity or distance data frame or 'dist' object
k	the k neighbourhood parameter
tau	the penalty parameter (suggested to be in [0,1])
type	what type of MDS to fit. Only "ratio" currently.
ndim	the dimension of the configuration
weightmat	a matrix of finite weights. Not implemented.
itmax	number of optimizing iterations, defaults to 5000.
init	initial configuration. If NULL a classical scaling solution is used.
verbose	prints info if > 0 and progress if > 1.
principal	If 'TRUE', principal axis transformation is applied to the final configuration
normconf	normalize the configuration to sum(delta^2)=1 (as in the power stresses). Note that then the distances in confdist do not match the manually calculated ones.

## Details

Note that k and tau are not independent. It is possible for normalized stress to become negative if the tau and k combination is so that the absolute repulsion for the found configuration dominates the local stress substantially less than the repulsion term does for the solution of  $D(X)=\Delta$ , so that the local stress difference between the found solution and perfect solution is nullified. This can typically be avoided if tau is between 0 and 1. If not, set k and or tau to a smaller value.

## Value

an object of class 'lmds' (also inherits from 'smacofP'). See [powerStressMin](#). It is a list with the components as in power stress

- delta: Observed, untransformed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized

- dhat: Explicitly transformed dissimilarities (dhats)
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- ndim: Number of dimensions
- model: Name of MDS model
- type: Is "ratio" here.
- niter: Number of iterations
- nobj: Number of objects
- pars: explicit transformations hyperparameter vector theta
- weightmat: 1-diagonal matrix (for compatibility with smacof classes)
- parameters, pars, theta: The parameters supplied
- call the call

and some additional components

- stress.m: default stress is the explicitly normalized stress on the normalized, transformed dissimilarities
- tau: tau parameter
- k: k parameter

### Author(s)

Lisha Chen & Thomas Rusch

### Examples

```
dis<-smacof::kinshipdelta
res<- lmds(dis,k=2,tau=0.1)
res
summary(res)
plot(res)
```

**mkBmat**

*Auxfunction1*

### Description

only used internally

### Usage

```
mkBmat(x)
```

### Arguments

x	matrix
---	--------

mkPower	<i>Take matrix to a power</i>
---------	-------------------------------

### Description

Take matrix to a power

### Usage

```
mkPower(x, r)
```

### Arguments

x	matrix
r	numeric (power)

### Value

a matrix

multiscale	<i>Multiscale SMACOF</i>
------------	--------------------------

### Description

An implementation for maximum likelihood MDS aka multiscale that minimizes the multiscale stress by majorization with ratio and interval optimal scaling. Uses a repeat loop. Note that since this done via the route of r-sytreess, the multiscale stress is approximate and only accuarte for kappa->0.

### Usage

```
multiscale(
  delta,
  type = c("ratio", "interval"),
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  kappa = 0.1,
  principal = FALSE
)
```

### Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances. Warning: these will get transformed to the log scale, so make sure that $\log(\text{delta}) \geq 0$ .
type	what optimal scaling type of MDS to fit. Currently one of "ratio" or "interval". Default is "ratio".
weightmat	a matrix of finite weights
init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.
itmax	maximum number of iterations. Default is 10000.
verbose	should iteration output be printed; if > 1 then yes
kappa	As this is not exactly multiscale but an r-stress approximation, we have multiscale only for $\kappa > 0$ . This argument can therefore be used to make the approximation more accurate by making it smaller. Default is 0.1.
principal	If 'TRUE', principal axis transformation is applied to the final configuration

### Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- delta: Observed dissimilarities
- tdelta: Observed explicitly transformed (log) dissimilarities, normalized
- dhat: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix
- stress.m: Default stress (stress-1^2)

### Warning

The input delta will internally get transformed to the log scale, so make sure that  $\log(\text{delta}) \geq 0$  otherwise it throws an error. It is often a good idea to use  $1+\text{delta}$  in this case.

### See Also

[rStressMin](#)

## Examples

```
dis<-smacof::kinshipdelta
res<-multiscale(as.matrix(dis),type="interval",itmax=1000)
res
summary(res)
plot(res)
```

**multistart**

*Multistart MDS function*

## Description

For different starting configurations, this function fits a series of PS models given in object or call and returns the one with the lowest stress overall. The starting configurations can be supplied or are generated internally.

## Usage

```
multistart(
  object,
  mdscall = NULL,
  ndim = 2,
  conflist,
  nstarts = 108,
  return.all = FALSE,
  verbose = TRUE,
  min = -5,
  max = 5
)
```

## Arguments

<b>object</b>	A fitted object of class 'smacofP', 'smacofB' or 'smacof'. If supplied this takes precedence over the call argument. If given this is added to the output and may be the optimal one.
<b>mdscall</b>	Alternatively to a fitted object, one can pass a syntactically valid call for any of the MDS functions cops, stops or smacof that find a configuration (not the ones that do parameter selection like pcops or stops). If object and call is given, object takes precedence.
<b>ndim</b>	Dimensions of target space.
<b>conflist</b>	Optional list of starting configurations.
<b>nstarts</b>	If conflist is not supplied, how many random starting configurations should be used. The default is 108, which implies that at least one of the stress is within the lowest 1 percent of all stresses with probability of 1/3 or within the lowest 5 percent of stresses with probability 0.996

<code>return.all</code>	Should all fitted MDS be returned. If FALSE (default) only the optimal one is returned.
<code>verbose</code>	If >0 prints the fitting progress.
<code>min</code>	lower bound for the uniform distribution to sample from
<code>max</code>	upper bound for the uniform distribution to sample from

## Details

If no configuration list is supplied, then nstarts configurations are simulated. They are drawn from a ndim-dimesnional uniform distribution with minimum min and maximum max. We recommend to use the route via supplying a fitted model as these are typically starting from a Torgerson configuration and are likely quite good.

One can simply extract `$best` and save that and work with it right away.

## Value

if 'return.all=FALSE', a list with the best fitted model as '`$best`' (minimal badness-of-fit of all fitted models) and '`$stressvec`' the stresses of all models. If 'return.all=TRUE' a list with slots

- `best`: The object resulting from the fit that had the overall lowest objective function value (usually stress)
- `stressvec`: The vector of objective function values
- `models`: A list of all the fitted objects.

## Examples

```
dis<-smacof::kinshipdelta

## Version 1: Using a fitted object (recommended)
res1<-rStressMin(delta=dis,type="ordinal",itmax=100)
resm<-multistart(res1,nstarts=2)
## best model
res2<-resm$best
#it's starting configuration
res2$init

## Version 2: Using a call object and supplying conflist
conflist<-list(res2$init,jitter(res2$init,1))
c1 <- call("rstressMin",delta=dis,type="ordinal",itmax=100)
resm<-multistart(mdscall=c1,conflist=conflist,return.all=TRUE)
```

---

<b>pdist</b>	<i>Squared p-distances</i>
--------------	----------------------------

---

**Description**

Squared p-distances

**Usage**

```
pdist(x, p)
```

**Arguments**

x	numeric matrix
p	p>0 the Minkowski distance

**Value**

squared Minkowski distance matrix

---

<b>permtest.smacofP</b>	<i>Permutation test for smacofP objects</i>
-------------------------	---

---

**Description**

Performs a permutation test on an MDS solution. It works with a smacofP object alone and also for derived dissimilarities, i.e. generated by the call dist(data). The original data matrix needs to be provided, as well as the type of dissimilarity measure used to compute the input dissimilarities.

**Usage**

```
## S3 method for class 'smacofP'
permtest(
  object,
  data,
  method.dat = "pearson",
  nrep = 100,
  verbose = FALSE,
  ...
)
```

## Arguments

object	Object of class smacofP if used as method or another object inheriting from smacof (needs to be called directly as permtest.smacofP then).
data	Optional: Initial data; if provided permutations are performed on the data matrix (see details)
method.dat	Dissimilarity computation used as MDS input. This must be one of "pearson", "spearmann", "kendall", "euclidean", "maximum", "manhattan", "canberra", "binary". If data is provided, then this must be provided as well.
nrep	Number of permutations.
verbose	If TRUE, bootstrap index is printed out.
...	Additional arguments needed for dissimilarity computation as specified in <a href="#">sim2diss</a> .

## Details

This routine permutes m dissimilarity values, where m is the number of lower diagonal elements in the corresponding dissimilarity matrix. For each sample a symmetric, nonmetric SMACOF of dimension 'ndim' is computed and the stress values are stored in 'stressvec'. Using the fitted stress value, the p-value is computed. Subsequently, the empirical cumulative distribution function can be plotted using the plot method.

If the MDS fit provided on derived proximities of a data matrix, this matrix can be passed to the 'permtest' function. Consequently, the data matrix is subject to permutations. The proximity measure used for MDS fit has to match the one used for the permutation test. If a correlation similarity is provided, it is converted internally into a dissimilarity using 'sim2diss' with corresponding arguments passed to the ... argument.

## Value

An object of class 'smacofPerm', see [permtest](#) for details and methods. It has values

- stressvec: Vector containing the stress values of the permutation samples
- stress.obs: Stress (observed sample)
- pval: Resulting p-value
- call: Model call
- nrep: Number of permutations
- nobj: Number of objects

## Examples

```
## see ?smacof::permtest for more
## permuting the dissimilarity matrix (full)
#' data(kinshipdelta)
fitkin <- rStressMin(kinshipdelta, ndim = 2, r=0.5,itmax=10) #use higher itmax
set.seed(222)
res.perm <- permtest(fitkin,nrep=5) #use higher nrep in reality
res.perm
plot(res.perm)
```

```

## permuting the data matrix
GOPdtm[ GOPdtm > 1 ] <- 1      ## use binary version
diss1 <- dist(t(GOPdtm[,1:10]), method = "binary")  ## Jaccard distance
fitgop1 <- alscal(diss1,type="interval",itmax=10) #use higher itmax
fitgop1
set.seed(123)
permtest(fitgop1, GOPdtm[,1:10], nrep = 5, method.dat = "binary")

```

**plot.smacofP***S3 plot method for smacofP objects*

## Description

S3 plot method for smacofP objects

## Usage

```

## S3 method for class 'smacofP'
plot(
  x,
  plot.type = "confplot",
  plot.dim = c(1, 2),
  bubscale = 1,
  col,
  label.conf = list(label = TRUE, pos = 3, col = 1, cex = 0.8),
  hull.conf = list(hull = FALSE, col = 1, lwd = 1, ind = NULL),
  shepard.x = NULL,
  identify = FALSE,
  type = "p",
  cex = 0.5,
  pch = 20,
  asp = 1,
  main,
  xlab,
  ylab,
  xlim,
  ylim,
  col.hist = NULL,
  legend = TRUE,
  legpos,
  loess = TRUE,
  shepard.lin = TRUE,
  ...
)

```

## Arguments

<code>x</code>	an object of class smacofP
<code>plot.type</code>	String indicating which type of plot to be produced: "confplot", "resplot", "Shepard", "stressplot", "transplot", "bubbleplot" (see details)
<code>plot.dim</code>	dimensions to be plotted in confplot; defaults to c(1, 2)
<code>bubscale</code>	Scaling factor (size) for the bubble plot
<code>col</code>	vector of colors for the points
<code>label.conf</code>	List with arguments for plotting the labels of the configurations in a configuration plot (logical value whether to plot labels or not, label position, label color)
<code>hull.conf</code>	Option to add convex hulls to a configuration plot. Hull index needs to be provided.
<code>shepard.x</code>	Shepard plot only: original data (e.g. correlation matrix) can be provided for plotting on x-axis
<code>identify</code>	If 'TRUE', the 'identify()' function is called internally that allows to add configuration labels by mouse click
<code>type</code>	What type of plot should be drawn (see also 'plot')
<code>cex</code>	Symbol size.
<code>pch</code>	Plot symbol
<code>asp</code>	Aspect ratio; defaults to 1 so distances between x and y are represented accurately; can lead to slightly weird looking plots if the variance on one axis is much smaller than on the other axis; use NA if the standard type of R plot is wanted where the ylim and xlim arguments define the aspect ratio - but then the distances seen are no longer accurate
<code>main</code>	plot title
<code>xlab</code>	label of x axis
<code>ylab</code>	label of y axis
<code>xlim</code>	scale of x axis
<code>ylim</code>	scale of y axis
<code>col.hist</code>	Color of the borders of the histogram.
<code>legend</code>	Flag whether legends should be drawn for plots that have legends
<code>legpos</code>	Position of legend in plots with legends
<code>loess</code>	if TRUE a loess fit (by Tukey's rescaling M-Estimator) of configuration distances explained by delta is added to the Shepard plot
<code>shepard.lin</code>	Shepard plot only: if TRUE the Shepard plot is linearized so $d^\kappa \sim \delta^\lambda$ . If FALSE $d \sim \delta^\lambda$
<code>...</code>	Further plot arguments passed: see 'plot.smacof' and 'plot' for detailed information.

## Details

- Configuration plot (`plot.type = "confplot"`): Plots the MDS configuration.
- Residual plot (`plot.type = "resplot"`): Plots the dhats  $f(T(\delta))$  against the transformed fitted distances  $T(d(X))$ .
- (Linearized) Shepard diagram (`plot.type = "Shepard"`): Is `shep.lin=TRUE` a diagram with the transformed observed normalized dissimilarities ( $T(\delta)$ ) on x against the transformed fitted distance ( $T(d(X))$  on y) as well as a loess curve and a regression line corresponding to type (linear without intercept for ratio, linear for interval and isotonic for ordinal). If `shep.lin=FALSE` it uses the untransformed delta. Note that the regression line corresponds to the optimal scaling results (`dhat`) only up to a linear transformation.
- Transformation Plot (`plot.type = "transplot"`): Diagram with normalized observed dissimilarities ( $\delta$ , light grey) and the normalized explicitly transformed dissimilarities ( $T(\Delta)$ , darker) against the untransformed fitted distances ( $d(X)$ ) together with a nonlinear regression curve corresponding to the explicit transformation (fitted power transformation). This is most useful for ratio models with power transformations as the transformations can be read off directly. For other MDS models and stresses, it still gives a quick way to assess how the explicit transformations worked.
- Stress decomposition plot (`plot.type = "stressplot"`): Plots the stress contribution in of each observation. Note that it rescales the stress-per-point (SPP) from the corresponding function to percentages (sum is 100). The higher the contribution, the worse the fit.
- Bubble plot (`plot.type = "bubbleplot"`): Combines the configuration plot with the point stress contribution. The larger the bubbles, the worse the fit.
- histogram ('`plot.type = "histogram"`'): gives a weighted histogram of the dissimilarities (weighted with `tweightmat` if exists else with `weightmat`). For optional arguments, see '`wtd.hist`'.

## Value

no return value; just plots for class 'smacofP' (see details)

## Examples

```
dis<-as.matrix(smacof::kinshipdelta)
res<-powerStressMin(dis)
plot(res)
plot(res,"Shepard")
plot(res,"resplot")
plot(res,"transplot")
plot(res,"stressplot")
plot(res,"bubbleplot")
plot(res,"histogram")
```

---

<code>powerStressFast</code>	<i>Power stress minimization by NEWUOA (<i>nloptr</i>)</i>
------------------------------	--

---

## Description

An implementation to minimize power stress by a derivative-free trust region optimization algorithm (NEWUOA). Much faster than majorizing as used in powerStressMin but perhaps less accurate.

## Usage

```
powerStressFast(
  delta,
  kappa = 1,
  lambda = 1,
  nu = 1,
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE
)
```

## Arguments

<code>delta</code>	dist object or a symmetric, numeric data.frame or matrix of distances
<code>kappa</code>	power of the transformation of the fitted distances; defaults to 1
<code>lambda</code>	the power of the transformation of the proximities; defaults to 1
<code>nu</code>	the power of the transformation for weightmat; defaults to 1
<code>weightmat</code>	a matrix of finite weights
<code>init</code>	starting configuration
<code>ndim</code>	dimension of the configuration; defaults to 2
<code>acc</code>	The smallest value of the trust region radius that is allowed. If not defined, then 1e-6 will be used.
<code>itmax</code>	maximum number of iterations. Default is 10000.
<code>verbose</code>	should iteration output be printed; if > 1 then yes

## Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- `delta`: Observed dissimilarities, not normalized
- `obsdiss`: Observed dissimilarities, normalized

- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1, square root of the explicitly normalized stress on the normalized, transformed dissimilarities)
- spp: Stress per point (based on stress.en)
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model

and some additional components

- gamma: Empty
- stress.m: default stress for the COPS and STOP. Defaults to the explicitly normalized stress on the normalized, transformed dissimilarities
- stress.en: explicitly stress on the normalized, transformed dissimilarities and normalized transformed distances
- deltaorig: observed, untransformed dissimilarities
- weightmat: weighting matrix

## See Also

[smacofSym](#)

## Examples

```
dis<-smacof::kinshipdelta
res<-powerStressFast(as.matrix(dis),kappa=2,lambda=1.5)
res
summary(res)
plot(res)
```

## Description

An implementation to minimize power stress by majorization with ratio or interval optimal scaling. Usually more accurate but slower than powerStressFast. Uses a repeat loop.

**Usage**

```
powerStressMin(  
    delta,  
    kappa = 1,  
    lambda = 1,  
    nu = 1,  
    type = "ratio",  
    weightmat = 1 - diag(nrow(delta)),  
    init = NULL,  
    ndim = 2,  
    acc = 1e-06,  
    itmax = 10000,  
    verbose = FALSE,  
    principal = FALSE  
)  
  
powerstressMin(  
    delta,  
    kappa = 1,  
    lambda = 1,  
    nu = 1,  
    type = "ratio",  
    weightmat = 1 - diag(nrow(delta)),  
    init = NULL,  
    ndim = 2,  
    acc = 1e-06,  
    itmax = 10000,  
    verbose = FALSE,  
    principal = FALSE  
)  
  
postmds(  
    delta,  
    kappa = 1,  
    lambda = 1,  
    nu = 1,  
    type = "ratio",  
    weightmat = 1 - diag(nrow(delta)),  
    init = NULL,  
    ndim = 2,  
    acc = 1e-06,  
    itmax = 10000,  
    verbose = FALSE,  
    principal = FALSE  
)  
  
pstressMin(  
    delta,
```

```

kappa = 1,
lambda = 1,
nu = 1,
type = "ratio",
weightmat = 1 - diag(nrow(delta)),
init = NULL,
ndim = 2,
acc = 1e-06,
itmax = 10000,
verbose = FALSE,
principal = FALSE
)

pStressMin(
  delta,
  kappa = 1,
  lambda = 1,
  nu = 1,
  type = "ratio",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

pstressmds(
  delta,
  kappa = 1,
  lambda = 1,
  nu = 1,
  type = "ratio",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

```

### Arguments

<code>delta</code>	dist object or a symmetric, numeric data.frame or matrix of distances
<code>kappa</code>	power of the transformation of the fitted distances; defaults to 1
<code>lambda</code>	the power of the transformation of the proximities; defaults to 1

nu	the power of the transformation for weightmat; defaults to 1
type	what type of MDS to fit. One of "ratio" or "interval". Default is "ratio".
weightmat	a matrix of finite weights or dist object
init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.
itmax	maximum number of iterations. Default is 10000.
verbose	should iteration output be printed; if > 1 then yes
principal	If 'TRUE', principal axis transformation is applied to the final configuration

### Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- delta: Observed, untransformed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized
- dhat: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- stress.m: Default stress (stress-1^2)
- tweightmat: transformed weightmatrix (here weightmat^nu)

### See Also

[smacofSym](#)

### Examples

```
dis<-smacof::kinshipdelta
res<-powerStressMin(dis,type="ratio",kappa=2,lambda=1.5,itmax=1000)
res
summary(res)
plot(res)
```

procruster

*procruster: a procrustes function***Description**

procruster: a procrustes function

**Usage**

procruster(x)

**Arguments**

x numeric matrix

**Value**

a matrix

rpowerStressMin

*Restricted Power Stress SMACOF***Description**

An implementation to minimize restricted power stress by majorization with ratio or interval optimal scaling. Restricted means that the same power is used for both dissimilarities and fitted distances. Uses a repeat loop.

**Usage**

```
rpowerStressMin(
  delta,
  expo = 1,
  nu = 1,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)
rpowerstressMin(
  delta,
```

```
    expo = 1,
    nu = 1,
    type = "ratio",
    weightmat,
    init = NULL,
    ndim = 2,
    acc = 1e-06,
    itmax = 10000,
    verbose = FALSE,
    principal = FALSE
)

rpostmds(
  delta,
  expo = 1,
  nu = 1,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

rpstressMin(
  delta,
  expo = 1,
  nu = 1,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

rpStressMin(
  delta,
  expo = 1,
  nu = 1,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
```

```

    acc = 1e-06,
    itmax = 10000,
    verbose = FALSE,
    principal = FALSE
  )

rpstressmds(
  delta,
  expo = 1,
  nu = 1,
  type = "ratio",
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

```

## Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances
expo	power of the transformation of the fitted distances and dissimilarities; defaults to 1
nu	the power of the transformation for weightmat; defaults to 1
type	what type of MDS to fit. One of "ratio" or "interval". Default is "ratio".
weightmat	a matrix of finite weights
init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.
itmax	maximum number of iterations. Default is 10000.
verbose	should iteration output be printed; if > 1 then yes
principal	If 'TRUE', principal axis transformation is applied to the final configuration

## Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- delta: Observed, untransformed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized
- dhat: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)

- spp: Stress per point
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- stress.m: Default stress (stress-1^2)
- tweightmat: transformed weightting matrix (here weightmat^nu)
- parameters, pars, theta: The parameter vector of the explicit transformations

## Examples

```
dis<-smacof::kinshipdelta
res<-rpowerStressMin(as.matrix(dis),expo=1.7,itmax=1000)
res
summary(res)
plot(res)
```

rStressMin

*R stress SMACOF*

## Description

An implementation to minimize r-stress by majorization with ratio, interval and ordinal optimal scaling. Uses a repeat loop.

## Usage

```
rStressMin(
  delta,
  r = 0.5,
  type = c("ratio", "interval", "ordinal"),
  ties = "primary",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)
rstressMin(
```

```

delta,
r = 0.5,
type = c("ratio", "interval", "ordinal"),
ties = "primary",
weightmat = 1 - diag(nrow(delta)),
init = NULL,
ndim = 2,
acc = 1e-06,
itmax = 10000,
verbose = FALSE,
principal = FALSE
)

rstressmds(
  delta,
  r = 0.5,
  type = c("ratio", "interval", "ordinal"),
  ties = "primary",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

rstress(
  delta,
  r = 0.5,
  type = c("ratio", "interval", "ordinal"),
  ties = "primary",
  weightmat = 1 - diag(nrow(delta)),
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)

```

## Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances
r	power of the transformation of the fitted distances (corresponds to kappa/2 in power stress); defaults to 0.5 for standard stress
type	what type of MDS to fit. Currently one of "ratio", "interval" or "ordinal". Default is "ratio".

<b>ties</b>	the handling of ties for ordinal (nonmetric) MDS. Possible are "primary" (default), "secondary" or "tertiary".
<b>weightmat</b>	a matrix of finite weights.
<b>init</b>	starting configuration
<b>ndim</b>	dimension of the configuration; defaults to 2
<b>acc</b>	numeric accuracy of the iteration. Default is 1e-6.
<b>itmax</b>	maximum number of iterations. Default is 10000.
<b>verbose</b>	should iteration output be printed; if > 1 then yes
<b>principal</b>	If 'TRUE', principal axis transformation is applied to the final configuration

### Value

a 'smacofP' object (inheriting from 'smacofB', see [smacofSym](#)). It is a list with the components

- delta: Observed, untransformed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized
- dhat: Explicitly transformed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- stress.m: Default stress (stress-1^2)
- tweightmat: transformed weighting matrix (here NULL)

### See Also

[smacofSym](#)

### Examples

```
dis<-smacof::kinshipdelta
res<-rStressMin(as.matrix(dis),type="ordinal",r=1,itmax=1000)
res
summary(res)
plot(res)
```

**sammon***Wrapper to sammon for S3 class*

## Description

Wrapper to *sammon* for S3 class

## Usage

```
sammon(d, y = NULL, k = 2, ...)
```

## Arguments

- d a distance structure such as that returned by 'dist' or a full symmetric matrix. Data are assumed to be dissimilarities or relative distances, but must be positive except for self-distance. This can contain missing values.
- y An initial configuration. If NULL, `cmdscale` is used to provide the classical solution. (If there are missing values in 'd', an initial configuration must be provided.) This must not have duplicates.
- k The dimension of the configuration
- ... Additional parameters passed to *sammon*, see [sammon](#)

## Details

Overloads MASS::*sammon* and adds new slots and class attributes for which there are methods.

## Value

Object of class 'sammonx' inheriting from [sammon](#). This wrapper adds an extra slot to the list with the call, adds column labels to the \$points, adds slots conf=points, delta=d, dhat=normalized dissimilarities, confdist=distance between points in conf, stress.m=stress, stress=sqrt(stress.m) and assigns S3 classes 'sammonx', 'sammon' and 'cmdscalex'.

## Examples

```
dis<-as.matrix(smacof::kinshipdelta)
res<-sammon(dis)
```

---

sammonmap*Sammon Mapping SMACOF*

---

## Description

An implementation to minimize Sammon stress by majorization with ratio and interval optimal scaling. Uses a repeat loop.

## Usage

```
 sammonmap(
  delta,
  type = c("ratio", "interval"),
  weightmat,
  init = NULL,
  ndim = 2,
  acc = 1e-06,
  itmax = 10000,
  verbose = FALSE,
  principal = FALSE
)
```

## Arguments

delta	dist object or a symmetric, numeric data.frame or matrix of distances
type	what type of MDS to fit. Currently one of "ratio" and "interval". Default is "ratio".
weightmat	a matrix of finite weights
init	starting configuration
ndim	dimension of the configuration; defaults to 2
acc	numeric accuracy of the iteration. Default is 1e-6.
itmax	maximum number of iterations. Default is 10000.
verbose	should iteration output be printed; if > 1 then yes
principal	If 'TRUE', principal axis transformation is applied to the final configuration

## Value

a 'smacofP' object (inheriting from smacofB, see [smacofSym](#)). It is a list with the components

- delta: Observed dissimilarities
- tdelta: Observed explicitly transformed dissimilarities, normalized
- dhat: Observed dissimilarities (dhats), optimally scaled and normalized
- confdist: Configuration dissimilarities
- conf: Matrix of fitted configuration

- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point (based on stress.en)
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix as supplied
- stress.m: default stress (stress-1^2)
- tweightmat: weighting matrix after transformation (here weightmat/delta)

### See Also

[rStressMin](#)

### Examples

```
dis<-smacof::kinshipdelta
res<-sammonmap(as.matrix(dis),itmax=1000)
res
summary(res)
plot(res)
```

scale_adjust	<i>Adjusts a configuration</i>
--------------	--------------------------------

### Description

Adjusts a configuration

### Usage

```
scale_adjust(conf, ref, scale = c("sd", "std", "proc", "none"))
```

### Arguments

conf	a configuration
ref	a reference configuration (only for scale="proc")
scale	Scale adjustment. "std" standardizes each column of the configurations to mean=0 and sd=1, "sd" scales the configuration by the maximum standard deviation of any column, "proc" adjusts the fitted configuration to the reference

### Value

The scale adjusted configuration.

---

secularEq*Secular Equation*

---

**Description**

Secular Equation

**Usage**

secularEq(a, b)

**Arguments**

a	matrix
b	matrix

---

smacofx

*smacofx: Flexible multidimensional scaling methods and SMACOF extensions*

---

**Description**

Flexible multidimensional scaling (MDS) methods centered around the Majorization algorithm. The package contains various functions, wrappers, methods and classes for fitting, plotting and displaying a large number of different flexible MDS models such as Torgerson scaling, ratio, interval and nonmetric MDS with majorization, Sammon mapping with ratio and interval optimal scaling, multiscale MDS with ratio and interval optimal scaling, Alscal (s-stress) MDS with ratio and interval optimal scaling, elastic scaling with ratio and interval optimal scaling, r-stress MDS for ratio, interval and nonmetric scaling, power stress for interval and ratio optimal scaling, restricted power-stress with ratio and interval optimal scaling, approximate power-stress with ratio scaling, curvilinear component analysis with ratio, interval and ordinal optimal scaling, power curvilinear component analysis with ratio, interval and ordinal optimal scaling, Box-Cox MDS and local MDS. Some functions are suitably flexible to allow any other sensible combination of explicit power transformations for weights, distances and input proximities with implicit ratio, interval or ordinal optimal scaling of the input proximities. Most functions use a majorization algorithm.

**Details**

The package provides:

Models:

- alscal... ALSCAL (s-stress) MDS with ratio, interval optimal scaling
- elscal.. Elastic scaling MDS with ratio, interval optimal scaling
- multiscale... Multiscale MDSwith ratio, interval optimal scaling

- rstressMin .. R-Stress MDS with ratio, interval, ordinal optimal scaling
- powerStressMin... power stress MDS (POST-MDS) with ratio, interval optimal scaling
- apStressMin... approximate POST-MDS with ratio, interval optimal scaling
- rpowerStressMin... restricted POST-MDS with ratio, interval optimal scaling
- clca ... curvilinear component analysis with ratio, interval, ordinal optimal scaling
- pclca ... power curvilinear component analysis with ratio, interval, ordinal optimal scaling
- bcmds ... Box-Cox MDS with ratio optimal scaling
- lmds... Local MDS with ratio optimal scaling
- sammonmap... Sammon mapping with ratio, interval optimal scaling

**Classes and Methods:** The objects are of classes that extend the S3 classes smacof and smacofB. For the objects returned by the high-level functions S3 methods for standard generics were implemented, including print, coef, residuals, summary, plot, plot3dstatic. Wrappers and convenience functions for the model objects:

- bootmds ... bootstrapping and MDS model
- biplotmds ... MDS Biplots
- icExploreGen ... Explore initial configurations
- jackmds ... jackknife for MDS
- multistart ... multistart function for MDS
- permtest ... permutation test for MDS

**Wrappers:**

- cmdscale ... stats::cmdscale but returns an S3 objects to be used with smacof classes
- sammon... MASS::sammon but returns S3 objects to be used with smacof classes

**Authors:** Thomas Rusch, Jan de Leeuw, Lisha Chen, Patrick Mair

**Maintainer:** Thomas Rusch

## Examples

```
data(BankingCrisesDistances)

res<-rStressMin(BankingCrisesDistances[,1:69],type="ordinal",r=2)
res

summary(res)
plot(res)
plot(res,"transplot")
plot(res,"Shepard")

msres<- multistart(res)

res2<-msres$best
permtest(res2)
```

---

spp	<i>Calculating stress per point</i>
-----	-------------------------------------

---

**Description**

Calculating stress per point

**Usage**

```
spp(dhat, confdist, weightmat)
```

**Arguments**

dhat	a dist object or symmetric matrix of dissimilarities
confdist	a dist object or symmetric matrix of fitted distances
weightmat	dist objetc or symmetric matrix of weights

**Value**

a list

---

sqdist	<i>Squared distances</i>
--------	--------------------------

---

**Description**

Squared distances

**Usage**

```
sqdist(x)
```

**Arguments**

x	numeric matrix
---	----------------

**Value**

squared distance matrix

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